

# MATH 451/551

## Chapter 5. Common Continuous Distribution

### 5.1 Uniform Distribution

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## Parameters

- ▶ **Location** (or shift) parameters
- ▶ **Scale** parameters are used to expand or contract the  $x$ -axis by a factor
- ▶ **Shape** parameters affect the shape of the probability density function



## Uniform Distribution

- ▶ A continuous random variable  $X$  is “uniformly distributed” between  $a$  and  $b$  if  $X$  is equally likely to assume any value on the interval  $(a, b)$ .
- ▶ A continuous random variable  $X$  with pdf

$$f(x) = \frac{1}{b-a}, \quad a < x < b$$

for real constants  $a$  and  $b$  satisfying  $a < b$  is a  $U(a, b)$  random variable.



# Mean



# Variance





# Skewness





# Kurtosis





## R Functions

Function	Returned Value
dunif(x, a, b)	calculates the probability density function $f(x)$
punif(x, a, b)	calculates the cumulative distribution function $F(x)$
qunif(u, a, b)	calculates the percentile (quantile) $F^{-1}(u)$
runif(m, a, b)	generates $m$ random variates

# Example 1



## Example 1

A shuttle train at a busy airport completes a circuit between two terminals every five minutes. What is the probability that a passenger will wait more than three minutes for a shuttle train?

## Example 2



### Example 2

What is the probability that the quadratic equation  $x^2 + Bx + 1 = 0$  has two real roots, where  $B \sim U(0, 3)$ ? (Hint: The quadratic equation  $ax^2 + bx + c = 0$  has two real roots if the discriminant  $b^2 - 4ac$  is positive.)

# Example 3



## Example 3

Let  $X \sim U(0, 1)$ , find  $V(3\lfloor 2X \rfloor + 4)$ .

## Example 4



### Example 4

Divide a line segment of unit length randomly into two parts. Find the expected value of the product of the lengths of the two segments.

# Thank You



THANK YOU!